

TB154405A

Reg. No:

Name:

B. Sc. DEGREE (C.B.C.S.S.) EXAMINATION, MARCH 2017
SEMESTER IV – COMPLEMENTARY COURSE (MATHEMATICS)
MT4CPC04B – FOURIER SERIES, DIFFERENTIAL EQUATIONS, NUMERICAL
ANALYSIS AND ABSTRACT ALGEBRA
(Common For Physics And Chemistry)

Time: Three Hours

Maximum Marks: 80

PART A

I. Answer all questions. Each question carries 1 mark.

1. Write the Rodrigue's formula for Legendre polynomial.
2. Is $e^{-|x|}$, $-\pi < x < \pi$, an even function or odd function.
3. Evaluate $f(1)$ using Taylor's series for $f(x) = x^3 - 3x^2 + 5x - 10$.
4. Define a group.
5. Define isomorphism.
6. What are the direction cosines normal to the surface $z = f(x, y)$ at the point (x, y, z) .

(6x1=6)

PART B

II. Answer any seven questions. Each question carries 2 marks.

7. What is the expression for $P_0(x)$, $P_2(x)$ and $P_4(x)$.
8. Write the first four Legendre polynomials.
9. Derive a partial differential equation by eliminating f and g from the relation
 $Z = f(x+ay) + g(x-ay)$
10. Define partial differential equation. Write the Lagranges partial differential equation.
11. Find the equation of the tangent to the surface $x^2 + y^2 + z^2 = 1$ at the point $(1/3, 2/3, -1)$.
12. Evaluate $S = \sqrt{3} + \sqrt{5} + \sqrt{7}$ to 4 significant digits and find its absolute and relative error.
13. Write the computational steps for false position method.
14. Define permutation of a set.
15. Write any one subgroup of klein 4-group $\{e, a, b, c\}$
16. Let $*$ be defined on Q^+ by $a * b = \frac{ab}{2}$. Prove that Q^+ is a group.

(7x2=14)

PART C

III. Answer any five questions. Each question carries 6 marks.

17. Find the fourier series of the function $f(x) = \begin{cases} -1, & \text{if } 0 < x < \frac{\pi}{2} \\ 0, & \text{if } \frac{\pi}{2} < x < 2\pi \end{cases}$
18. Find series solution of the equation $(1-x^2)y'' - 2xy' + 2y = 0$.

19. Find the integral curves of $\frac{dx}{x(y-z)} = \frac{dy}{y(z-x)} = \frac{dz}{z(x-y)}$.
20. Find the general integral of $y^2p - xyq = x(z - 2y)$.
21. Using Newton-Raphson method find a positive real root of $x^3 - 6x + 4 = 0$.
22. Given $f(x) = \sin x$, construct the Taylor series approximations of orders 0 to 4 at $x = \frac{\pi}{3}$ and state their absolute errors.
23. Prove that the subgroup of a cyclic group is cyclic.
24. Write the group table for the 4th dihedral group, D_4 .

(5x6=30)

PART D

IV. Answer any two questions. Each question carries 15 marks.

25. (i) State and prove Cayley's theorem.
(ii) Show that the set of all complex numbers with usual addition and multiplication is a field.
26. (i) Use method of iteration to find the root of $xe^x = 1$, with an accuracy of 10^{-4} .
(ii) Find a root of the equation $x^2 - 4x - 10 = 0$ using bisection method.
27. (i) Find the general solution of $px(z-2y^2) = (z-xy)(z^2-y^2-2x^3)$.
(ii) Solve $\frac{dx}{x+z} = \frac{dy}{y} = \frac{dz}{z+y^2}$
28. Find the Fourier cosine series and Fourier sine series for the function $f(x) = -x$, $0 < x < \pi$.

(2x15=30)