

BACHELOR'S DEGREE EXAMINATION, OCTOBER 2025
2025 ADMISSIONS REGULAR
SEMESTER I - MINOR - B (MATHEMATICS)
MT12SCB101B24 - Ground Roots of Mathematics

Time : 1.5 Hours

Maximum Marks : 50

Part A

Answer all questions. Each question carries 1 mark.

(1x10=10)

1. Estimate the cardinality of the set $\{2,4,6,8,10\}$ [CO1,Understand]
2. Define a singleton set. [CO1,Remember]
3. List the members of the set $A = \{x \mid x \text{ is a real number such that } x^2 = 1\}$. [CO1,Remember]
4. Illustrate $y = x^{-5}$ is an odd function. [CO2,Understand]
5. Estimate $(f - g)(x)$, given $f(x) = 5x + 3$ and $g(x) = x + 3$. [CO2,Understand]
6. Calculate $f(g(0))$ where $f(x) = x + 5$ and $g(x) = x$. [CO2,Apply]
7. If $f(x) = \tan^2 x$, Determine $f'(x)$. [CO3,Apply]
8. Calculate $\frac{dy}{dx}$, if $y = x^2 + \sin x$. [CO3,Apply]
9. $y = x \sin x$. Determine $\frac{dy}{dx}$. [CO3,Apply]
10. Identify which critical points of the function $f(x) = 3x^3 + 12x$ are stationary points. [CO4,Understand]

Part B

Answer any 2 questions from the bunch of CO1. Each question carries 5 mark.

(2x5=10)

11. Illustrate using a Venn Diagram the set of vowels V in the English alphabet. [CO1,Understand]
12. Estimate the cardinality of the following sets
 $A = \{1, 3, 5, 7, 9\}$
 $B = \{a, b, c\}$
 $A \cup B$
 $A \cap B$
 $A - B$ [CO1,Understand]
13. Let $A = \{1,2,3\}$, $B = \{x, y\}$, $C = \{a, b\}$. Express as a set a) $A \times B$ b) $B \times C$ c) $A \times C$ d) $A \times B \times C$. Describe how many elements does $A \times B \times C$ have if A has m elements, B has n elements and C has p elements. [CO1,Understand]

Part C

Answer any 2 questions from the bunch of CO2. Each question carries 5 mark.

(2x5=10)

14. Determine the domain and range of the function $f(x) = 1 + x^2$. [CO2,Apply]
15. Determine $f(g(2))$ and $g(g(1))$ where $f(x) = 3x + 4$ and $g(x) = 2x - 1$. [CO2,Apply]
16. Compute $f \circ g$ and $g \circ f$ if $f(x) = x - 6$ and $g(x) = 5x$. [CO2,Apply]

Part D

Answer any 1 question from the bunch of CO3. Each question carries 5 mark.

(1x5=5)

17. Illustrate that if $x \neq 0$ then $y = 1/x$ satisfies the equation $x^2y'' + x^2y' - xy = 0$. [CO3,Apply]

18. Determine $\frac{d}{dx} (2x^6 + x^{-9})$. [CO3,Apply]

19. Calculate $\frac{d}{dx} [\sin(1 + \cos x)]$. [CO3,Apply]

Part C

Answer any 1 question from the bunch of CO4. Each question carries 10 mark. (10x1=10)

20. (a) Determine the intervals on which $f(x) = x^2 - 3x + 8$ is concave up and concave down.
(b) Calculate the relative extrema of the function $f(x) = 3x^5 - 5x^3$. [CO4,Analyse]

21. (a) Determine the intervals where the function $f(x) = x^2 + 2x + 1$ is increasing or decreasing.
(b) Deduce the absolute maximum and minimum values of the function $f(x) = 6x^{4/3} - 3x^{1/3}$ on the interval $[-1, 1]$. [CO4,Analyse]