

TH241325MINC

Reg. No.....

Name.....

FYUG PROGRAMME EXAMINATIONS, NOVEMBER 2024

(2024 Admission Regular)

SEMESTER I – MINOR C COURSE (MATHEMATICS)

MT1DSCB101B24-GROUND ROOTS OF MATHEMATICS

Time: 1.5 Hours

Maximum Marks: 50

PART A

I. Answer all questions (MCQ). Each question carries 1 mark

| Q.No: | QUESTIONS | CO | LEVEL |
|-------|---|----|-------|
| 1. | Identify the false statement. (a) $\emptyset \in \{\emptyset\}$ (b) $\emptyset \in \{\emptyset, \{\emptyset\}\}$ (c) $\{\emptyset\} \in \{\{\emptyset\}\}$ (d) $\{\emptyset\} \subset \{\emptyset, \{\emptyset\}\}$ | 1 | R |
| 2. | Select an odd function (a) $f(x) = 3$ (b) $g(x) = x^4 + 3x^2 - 1$ (c) $f(x) = x^2 + 1$ (d) $f(x) = x^{-5}$ | 1 | R |
| 3. | Determine $\frac{d}{dx} (2x^6 + x^{-9})$. (a) $12x^5 - 9x^{-10}$ (b) $8x^5 - 9x^{-10}$ (c) $12x^5 - 9x^{-8}$ (d) $12x^5 + 9x^{-10}$ | 3 | Ap |
| 4. | Compute $f'(x)$, if $f(x) = \cos^2 x$ (a) $-2\sin x \cos x$ (b) $2\sin x \cos x$ (c) $\sin x \cos x$ (d) $-\sin^2 x$ | 3 | Ap |
| 5. | Identify the true statement regarding a function $f(x)$ with critical point at $x = c$. (a) $f(c)=0$ (b) $f'(c) = 0$ or $f'(c)$ is undefined (c) $f(c)$ must be a maximum or minimum (d) $f''(c) = 0$ | 4 | U |

(5x1=5)

II. Answer all questions in one word. Each question carries 1 mark

| Q.No: | QUESTIONS | CO | LEVEL |
|-------|--|----|-------|
| 6. | State the number of elements in $A \times B$ when set A has m elements and set B has n elements. | 1 | R |
| 7. | Write the derivative of a constant function. | 3 | Ap |
| 8. | Calculate $(f \circ g)'(2)$, if $f'(9) = 5$, $g(2) = 9$ and $g'(2) = -3$ | 3 | Ap |
| 9. | Compute $f'(x)$, if $f(x) = x$ | 3 | Ap |

| | | | |
|-----|--|---|---|
| 10. | Identify the critical points of $f(x) = 1 - x^5$. | 4 | U |
|-----|--|---|---|

(5x1=5)

PART B

III. Answer any six questions in one paragraph. Each question carries 5 marks.

| Q.No: | QUESTIONS | CO | LEVEL |
|-------|--|----|-------|
| 11. | 1) Let $A = \{a, b, c, d\}$, $B = \{y, z\}$. Determine $A \times B$. 2) Let $A = \{0, 2, 4, 6, 8, 10\}$, $B = \{0, 1, 2, 3, 4, 5, 6\}$ and $C = \{4, 5, 6, 7, 8, 9, 10\}$. Determine $(A \cup B) \cap C$. | 2 | Ap |
| 12. | Determine the inverse of the function $y = (1/2)x + 1$ and express it in terms of x . | 2 | Ap |
| 13. | Calculate the points at which the graph of $y = x^3 - 3x + 4$ has a horizontal tangent line. | 3 | Ap |
| 14. | Establish that $y = x^3 + 3x + 1$ satisfies $y''' + xy'' - 2y' = 0$ | 3 | Ap |
| 15. | Compute $f'(x)$, if $f(x) = \frac{5 - \cos x}{5 + \sin x}$ | 3 | Ap |
| 16. | Compute $\frac{d^2y}{dx^2}$, if $y + \sin y = x$ using implicit differentiation. | 31 | Ap |
| 17. | Identify the intervals on which the function $f(x) = x^2 - 4x + 3$ is increasing and the intervals on which it is decreasing. | 4 | U |
| 18. | Determine the absolute maximum and minimum values of the function $f(x) = 8x - x^2$ on the interval $[0, 6]$. | 5 | Ap |

(6x5=30)

PART C

IV. Answer any one question. The question carries 10 marks.

| Q.No: | QUESTIONS | CO | LEVEL |
|-------|--|------|-------|
| 19. | 1) Using Venn diagram illustrate $A \cap B$ where $A = \{1, 3, 5\}$ and $B = \{1, 2, 3\}$ 2) Sketch the graph of the greatest integer function. 3) Determine the derivative, given $f(x) = \frac{3x+4}{x^2+1}$. | 2, 3 | Ap |
| 20. | 1) Determine the intervals on which $f(x) = x^3 - 3x^2 + 1$ is increasing, decreasing, concave up and concave down. 2) Compute $f'(x)$ if $f(x) = \frac{\sin x}{x^2 + \sin x}$. | 4, 3 | Ap |

(1x10=10)

CO : Course Outcomes Level : R – Remember, U – Understand, Ap- Apply, An- Analyze, E- Evaluate, C- Create