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## B. Sc. DEGREE (C.B.C.S.S.) EXAMINATION, JANUARY 2019 (2016 Admission Supplementary) **SEMESTER V- CORE COURSE (MATHEMATICS) MT5B06B – DIFFERENTIAL EQUATIONS**

#### **Time: Three Hours**

**Maximum Marks: 80** 

#### PART A

#### I. Answer all. Each one carries 1 mark.

- 1. Define Bernoulli differential equation.
- Find the integrating factor of the equation  $\frac{dx}{dy} + \frac{2}{y}x = y^2$ . 2.
- 3. Write the UC set of the function  $x^2 e^{4x} \sin x$ .
- 4. Solve  $\frac{d^2y}{dr^2} 3\frac{dy}{dr} + 2y = 0$ .
- Define ordinary point of a second order differential equation. 5.
- The direction cosines of the normal to the surface z = f(x, y) at the point (x, y, z) are 6.

(6×1=6)

#### PART B

#### **II.** Answer any seven questions. Each one carries 2 marks.

- 7. Solve (3x + 2y)dx + (2x + y)dy = 0.
- 8. Solve  $\frac{dy}{dx} + \frac{y}{x} = x^2$ .
- 9. Write the UC set of the functions  $x^3e^{5x} \sin x$ ,  $x^5e^{2x}$ .
- 10. Show that  $e^{-x}$ ,  $e^{3x}$ ,  $e^{4x}$  are linearly independent solution of the differential equation

$$\frac{d^2y}{dx^3} - 6\frac{d^2y}{dx^2} + 5\frac{dy}{dx} + 12y = 0.$$
  
11. Solve  $\frac{d^2y}{dx^2} - 4\frac{dy}{dx} + 13y = 0.$ 

- 12. Locate and classify the singular points of  $(x^3 + x^2)\frac{d^2y}{dx^2} + (x^2 2x)\frac{dy}{dx} + 4y = 0$ . 13. Show that  $J_{-p}(x) = (-1)^p J_p(x)$ , if p is an integer.
- 14. Evaluate :
- $(D-1)(D-2)(t^2+e^t).$ i)
- ii)  $(D^2 + 3D)(e^{3t} + \cos t)$ .
- 15. Form the partial differential equation  $F(x^2y^2z^2, xyz) = 0$ .
- 16. Find the equation of the tangent plane to the surface  $x^2 + y^2 + z^2 = 1$  at the point  $\left(\frac{1}{\sqrt{14}},\frac{2}{\sqrt{14}},\frac{-1}{\sqrt{14}}\right)$

PART C

# $(7 \times 2 = 14)$

#### III. Answer any five questions. Each one carries 6 marks.

- 17. Solve (x + 2y + 3)dx + (2x + 4y 1)dy = 0.
- 18. Solve  $\frac{dy}{dx} + y = xy^3$ .

- 19. Solve  $\frac{d^2y}{dx^2} + 4y = \sec^2 2x.$
- 20. Given that y = x is a solution of  $(x^3 x + 1)\frac{d^2y}{dx^2} + (x^2 + x)\frac{dy}{dx} + (x + 1)y = 0$ . Find a linearly independent solution by reducing the order. Find the general solution.
- 21. Solve  $x^2 \frac{d^2 y}{dx^2} 4x \frac{dy}{dx} + 4y = 4x^2 6x^3$ .

22. Find the power series solution of the differential equation  $\frac{d^2y}{dx^2} + x\frac{dy}{dx} + y = 0$ .

23.  $J_p(x)$  is the solution of the Bessel's equation of order p. Then show that :

i) 
$$\frac{d}{dx}(x^p J_p(x)) = x^p J_{p-1}(x)$$

ii) 
$$\frac{d}{dx}(x^{-p}J_p(x)) = x^{-p}J_{p+1}(x)$$

24. Find the general integral of  $y^2p - xyq = x(z - 2y)$ .

(5×6=30)

#### PART D

### IV. Answer any two questions. Each one carries 15 marks.

25. Solve the differential equation (x - 2y - 3)dx + (2x + y - 1)dy = 0.

26. Solve 
$$\frac{d^2y}{dx^2} - 3\frac{dy}{dx} + 2y = x^2e^x$$
.

27. Find the general solution of  $(x^2 - 1)y'' - 2xy' + 2y = (x^2 - 1)^2$ .

28. Find the general solution of the linear system of equations:

$$2\frac{dx}{dt} - 2\frac{dy}{dt} - 3x = t$$
$$2\frac{dx}{dt} + 2\frac{dy}{dt} + 3x + 8y = 2$$

(2×15=30)