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B. Sc. DEGREE (C.B.C.S.S.) EXAMINATION, NOVEMBER 2024 (2016 & 2017 Admission Supplementary) SEMESTER V- CORE COURSE (MATHEMATICS) MT5B08B - GRAPH THEORY

Time: Three Hours Maximum Marks: 80

PART A

- I. Answer all the questions. Each question carries 1mark.
- 1. State True or False: "Every trail is a path."
- 2. Draw the complement of K_3
- 3. Give an example of a tree with 5 edges.
- 4. Give an example of a complete bipartite graph.
- 5. Give an example of a perfect matching.
- 6. Define a tournament.

(6x1=6)

PART B

- II. Answer any seven questions. Each question carries 2 marks.
- 7. Draw two spanning subgraphs of K_4
- 8. Find the radius and diameter of the Petersen graph.
- 9. Define incidence matrix of a graph. What is the sum of the elements of its ithrow?
- 10. Let G be a connected graph. Then prove that G is a tree if and only if for every edge of Gis a bridge.
- 11. State the first theorem of Digraph theory.
- 12. Define closure of a simple graph.
- 13. State Redei's theorem.
- 14. Define cut vertex of a graph with an example.
- 15. Define Hamiltonian graph with an example.
- 16. Define an Euler digraph.

(7x2 = 14)

PART C

- III. Answer any five questions. Each question carries 6 marks.
- 17. For any two vertices u and v of a graph G, prove that every u-v walk contains a u-v path.
- 18. Explain Chinese Postman Problem.
- 19. Define closure of a graph and prove that a simple graph G is Hamiltonian if and only if its closure is Hamiltonian.





- 20. Let D be a weakly connected digraph with at least two vertices. If D has two vertices u and v such that od(u) = id(u) + 1 and id(v) = od(v) + 1 and, for all other vertices w of D, od(w) = in(w) then prove that D has a directed Euler trail
- 21. Explain the Personnel Assignment problem.
- 22. Explain Konisberg bridge problem.
- 23. Draw the four tournaments on 4 vertices.
- 24. Define orientation of a graph and draw all the possible orientations of K₃. How many of them are strongly connected?

(5x6=30)

PART D

- IV. Answer any two questions. Each question carries 15 marks.
- 25. Prove that a non- empty graph G with at least two vertices is bipartite if and only if it has no odd cycles.
- 26. State and prove Whitney's theorem.
- 27. a) Explain Marriage problem.
 - b) Let G be a k-regular bipartite graph with k > 0. Then prove that G has a perfect matching.
- 28. Show that a weakly connected digraph D with at least one arc is Euler if and only if od(v)=id(v) for every vertex 'v' of D.

(2x15=30)

