

B. Sc. DEGREE (C.B.C.S.) EXAMINATION, NOVEMBER 2022
(2020 Admission Regular and 2019, 2018 Admission Supplementary)
SEMESTER V - CORE COURSE (MATHEMATICS)
(Common for Mathematics and Computer Applications)

Time : 3 Hours

MT5B07B18 - DIFFERENTIAL EQUATIONS

Maximum Marks : 80

Part A

I. Answer any Ten questions. Each question carries 2 marks

(10x2=20)

1. Write the formula to find the oblique trajectories intersecting a given family of curves at an angle α .
2. Identify the linearity of the differential equation $y^2 \frac{d^2 y}{dx^2} + 5y = 0$ and illustrate the reasons.
3. Recall on what factor does the number of arbitrary constants in the general solution of a differential equation depend.
4. Evaluate the wronskian and check whether e^x and e^{2x} are linearly independent.
5. Solve $\frac{d^2 y}{dx^2} - 6\frac{dy}{dx} + 9y = 0$.
6. Solve $\frac{d^2 y}{dx^2} - 5\frac{dy}{dx} + 6y = 0$.
7. Evaluate the general solution $4\frac{d^2 y}{dx^2} + 4\frac{dy}{dx} + y = 0$.
8. State the two conditions to check the regularity of singular points
9. Define regular singular points.
10. Determine the nature of the point $x=0$ of the equation $\frac{d^2 y}{dx^2} + y \sin x = 0$.
11. Write the partial differential equation $ax^2 + by^2 + z^2 = 1$.
12. Write the partial differential equation $z = (x+a)(y+b)$.

Part B

II. Answer any Six questions. Each question carries 5 marks

(6x5=30)

13. Solve $x \sin y dx + (x^2 + 1) \cos y dy = 0$.
14. Determine the oblique trajectories that intersect the family of straight lines $y = cx$ at an angle 45° .
15. Solve $\frac{d^2 y}{dx^2} - 4\frac{dy}{dx} + 3y = 9x^4 + 4$.
16. Solve $x^3 \frac{d^3 y}{dx^3} - 4x^2 \frac{d^2 y}{dx^2} + 8x \frac{dy}{dx} - 8y = 4 \ln x$.
17. Classify the singular points of $(x^5 + x^4 - 6x^3) \frac{d^2 y}{dx^2} + x^2 \frac{dy}{dx} + (x-2)y = 0$.
18. Compute the power series solution of $\frac{d^2 y}{dx^2} + 8x \frac{dy}{dx} - 4y = 0$.

19. Compute the power series solution in powers of x of the differential equation $\frac{d^2y}{dx^2} - x\frac{dy}{dx} - y = 0$.
20. Solve the partial differential equation $p\sqrt{x} + q\sqrt{y} = \sqrt{z}$
21. If $z = f(x^2 - y) + g(x^2 + y)$. Show that $\frac{\partial^2 z}{\partial x^2} - \frac{1}{x}\frac{\partial z}{\partial x} = 4x^2\frac{\partial^2 z}{\partial y^2}$.

Part C

III. Answer any Two questions. Each question carries 15 marks

(2x15=30)

22. a) Solve $\frac{dy}{dx} + \left(\frac{2x+1}{x}\right)y = e^{-2x}$.

b) Solve $y^2 dx + (3xy - 1) dy = 0$.

23. a) Determine the general solution of the differential equation $x^2\frac{d^2y}{dx^2} - 5x\frac{dy}{dx} + 8y = 2x^3$.

b) Solve the differential equation $\frac{d^2y}{dx^2} + 4y = \sec^2 2x$ by the method of variation of parameters.

24. Solve $2x\frac{d^2y}{dx^2} + \frac{dy}{dx} + 2y = 0$ using the method of Frobenius.

25. a) $x^2(y - z)p + y^2(z - x)q = z^2(x - y)$
 b) $(x^2 - y^2 - z^2)p + 2xyq = 2xz$.