

TB221340V

Reg. No :

Name :

B.Sc. DEGREE (C.B.C.S.) EXAMINATION, NOVEMBER 2022

(2022 Admissions (regular) 2021 Admissions (Improvement / Supplementary), 2020, 2019, 2018, Admissions Supplementary)

SEMESTER I - CORE COURSE (MATHEMATICS) (Common For Mathematics and CA)

Time : 3 Hours MT1B01B18 - DISCRETE MATHEMATICS AND TRIGONOMETRY Maximum Marks : 80

Part A

I. Answer any Ten questions. Each question carries 2 marks (10x2=20)

1. Define tautology and contradiction.
2. Calculate the bitwise AND and bitwise XOR of the bit strings 011 011 011 0 and 110 001 110 1
3. Write the negation of the statement $\exists x(x^2 = 2)$.
4. State Domination laws with regard to set operations
5. Examine whether the function $f(x) = x^2$ from the set of integers to the set of integers onto
6. Define Symmetric Difference of two sets A and B . Find the symmetric difference of $A = \{1, 3, 5\}$ and $B = \{1, 2, 3\}$
7. Define a well ordered set. Determine whether the set of integers with usual less than or equal to relation is a well ordered set.
8. Explain the terms greatest lower bound and least upper bound relative to a partial order relation
9. Determine whether $\{1, 2, 5, 10, 30\}$ is a chain under divisibility relation
10. Write the Gregory's series
11. Compute the period of $\sin x$.
12. Write the infinite series expansion of e^x .

Part B

II. Answer any Six questions. Each question carries 5 marks (6x5=30)

13. Write a direct proof for the theorem "If m and n are both perfect squares, then mn is also a perfect square"
14. Let p, q and r be the propositions
p: You have the flu
q: You miss the final exam
r: You pass the course
Express the proposition $(p \wedge q) \vee (\neg q \wedge r)$ as an English sentence.
15. Give examples of the following functions (a). one- one but not onto (b). Not one- one but onto (c). One- one and onto (d). neither one-one nor onto
16. Define floor and ceiling function and sketch the graph of these functions.
17. Let Z be the set of all integers. Define $R = \{(a, b) \mid b = a^r\}$ for some positive integer r. Show that R is a partial ordering of Z.
18. Construct Hasse diagram for the poset $(\{1, 2, 3, 6, 12\}, /)$ where '/' is the divided relation. Also determine whether the poset is totally ordered
19. Factorise $x^7 - 1$ into real factors

20. If $\log \sin(x + iy) = a + ib$, show that $2e^{2a} = \cosh 2y - \cos 2x$

21. Show that the sum of the series $\sinh \alpha - \frac{1}{2} \sinh 2\alpha + \frac{1}{3} \sinh 3\alpha - \dots = \frac{\alpha}{2}$

Part C

III. Answer any Two questions. Each question carries 15 marks

(2x15=30)

22. (a). Show that $\sqrt{2}$ is irrational by giving a proof by contradiction

(b). Write a direct proof for the theorem "The sum of two rational numbers is rational"

23. (a). Show that if x is a real number $[2x] = [x] + \left[x + \frac{1}{2}\right]$.

(b). Let f be a function from A to B and let S and T be subsets of A . Show that

$$f^{-1}(S \cup T) = f^{-1}(S) \cup f^{-1}(T)$$

24. (a) Let D_{24} be the set of all divisors of 24 and let R be the relation defined by aRb if and only if a divides b . List all elements in R .

(b). Construct the Hasse diagram of D_{24} and find out the greatest element and least element.

(c). Determine whether the poset is a lattice

25. (a) If $-1 < r < 1$, show that $\sum_{n=1}^{\infty} r^n \sin nx = \frac{r \sin x}{1 - 2r \cos x + r^2}$

(b). Express $x^8 + 1$ as a product of real factors