TM211910TR	Reg. No :
	Name :

### M. Sc. DEGREE (C.S.S.) EXAMINATION, NOVEMBER 2021

[ 2021 Admissions Regular and 2020 Admissions Improvement & Supplementary ]
SEMESTER I - CORE COURSE (APPLIED STATISTICS AND DATA ANALYTICS)
ST1C03TM - ANALYTICAL TOOLS FOR STATISTICS

Time: 3 Hours Maximum Weight: 30

#### Part A

# I. Answer any Eight questions. Each question carries 1 weight

(8x1=8)

- 1. Define basis and dimension of basis.
- 2. Define norm of a vector.
- 3. State and prove completion theorem.
- 4. Explain row and column space of a matrix.
- 5. Show that every non-singular matrix is a product of elementary matrices.
- 6. Explain spectral representation of a real symmetric matrix.
- 7. State Cayley- Hamilton theorem.
- 8. Explain Moore Penrose inverse of a matrix.
- 9. Distinguish between unitary similarity and Orthogonal similarity.
- 10. Distinguish between positive definite matrix and positive semi definite matrix.

#### Part B

# II. Answer any Six questions. Each question carries 2 weight

(6x2=12)

- 11. Show that a non-singular matrix is a product of elementary matrices.
- 12. Examine the linear independence of the vectors (2, 1, 4), (0, 1, 4), (6, -1, 14).
- 13. Solve the linear system of equations, x+y+z=0, 2x-y+z=0, 3x+2z=0.
- 14. Find the inverse of the matrix by elementary transformation. A =  $\begin{bmatrix} 1 & 2 & 0 \\ 0 & 1 & 1 \\ 2 & 0 & 1 \end{bmatrix}$ .
- 15. Show that if  $\lambda$  is a characteristic root of A the  $\lambda^k$  is a characteristic root of  $A^k$ .
- 16. Using Cayley –Hamilton theorem obtain the inverse of the matrix  $\begin{bmatrix} 6 & -2 & 0 \\ -2 & 3 & 0 \\ 0 & 0 & 2 \end{bmatrix}$ .
- 17. If A is a real symmetric matrix, the show that |A| is the product of characteristic root and trace (A) is the sum of characteristic roots.
- 18. Reduce the quadratic form to the canonical form. Also give the linear transformation.  $x^2+2xy+2y^2-xz+z^2$ .

### Part C

19. 1. Find the non-singular matrices P and Q such that PAQ = 
$$\begin{bmatrix} \mathbf{I}_r & 0 \\ 0 & 0 \end{bmatrix}$$
 where A = 
$$\begin{bmatrix} 1 & 0 & -1 \\ 1 & 1 & 1 \\ 1 & 2 & -1 \\ 2 & 3 & 0 \end{bmatrix}$$

- 20. State and prove Rank-Nullity theorem.
- 21. State and prove Jacobi's theorem.
- 22. Examine the definiteness of the quadratic form  $6x^2 + 3y^2 + 14z^2 + 4yz + 18xz + 4xy$  after reducing it to its canonical form.